

Chapter 4

Integrals

4.5 The Substitution Rule

Example to start. Find the indefinite integral of $2x\sqrt{1+x^2}$, that is compute

$$\int 2x\sqrt{1+x^2} dx.$$

Example, Take 2. Compute the indefinite integral

$$\int 2x\sqrt{1+x^2} dx.$$

Substitution Rule. If $u = g(x)$ is a differentiable function whose range is an interval I and f is continuous on I , then

$$\int f'(g(x))g'(x) dx = \int f(u) du.$$

Relation between du and dx :

EXAMPLE 1 Find $\int x^3 \cos(x^4 + 2) dx$.

EXAMPLE 2 Evaluate $\int \sqrt{2x + 1} \, dx$.

EXAMPLE 3 Find $\int \frac{x}{\sqrt{1 - 4x^2}} \, dx$.

EXAMPLE 5 Find $\int \sqrt{1 + x^2} \, x^5 \, dx$.

EXAMPLE 7 Evaluate $\int_1^2 \frac{dx}{(3 - 5x)^2}$.