

# MATH 241

## CHAPTER 5

### SECTION 5.1: AREA BETWEEN CURVES

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## NON INTERSECTING REGIONS

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Desmos: <https://www.desmos.com/calculator/o7vvfgfwzy>

Given two functions  $f(x)$  and  $g(x)$  such that

$$g(x) \leq f(x) \quad a \leq x \leq b,$$

the area of the region  $S$  enclosed by  $f(x)$ ,  $g(x)$ ,  $x = a$  and  $x = b$  is

$$\text{AREA}(S) = \int_a^b f(x) - g(x) \, dx.$$

**EXAMPLE 1.** Find the area of the region bounded above by  $y = x^2 + 1$ , bounded below by  $y = x$ , and bounded on the sides by  $x = 0$  and  $x = 1$ .

## INTERSECTING REGIONS

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**EXAMPLE 2.** Find the area of the region enclosed by the functions  $y = x^2$  and  $y = x + 2$ .

General Steps:

1. Draw a picture and find the points of intersection between the two curves.
2. Set up the definite integral and evaluate the definite integral.

**EXAMPLE 3.** Find the area of the region enclosed by the line  $y = x - 1$  and the parabola  $y^2 = 2x + 6$ .

**EXAMPLE 4.** Find the area enclosed by the line  $y = x - 1$  and the parabola  $y^2 = 2x + 6$ .